# Invasive Weed Optimization Algorithm for Solving Multi-Objective Sequence-Dependent U-Shaped Disassembly Line Balancing Problem

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## ABSTRACT

Environmental protection has become a global problem since the deteriorating environment greatly threatens human existence. Due to rapid developments in technology and manufacturing methods, the number of waste products is increasing faster than ever. Product recovery is one of the most effective strategies to deal with the waste problem. Compared to the traditional landfilling, product recovery adds green concept in dealing with the waste problem as well as retrieving valuable parts and materials from end-of-life (EOL) products. Popular choices in product recovery are remanufacture, reuse, and recycle. Disassembly is an unavoidable step in remanufacturing and is an essential step in its profit-based objectives. With a higher line efficiency and flexibility, U-shaped disassembly line has many more advantages compared to the traditional straight-line disassembly line. In order to optimize the disassembly operations, it is necessary to solve the disassembly line balancing problem (DLBP). The DLBP involves optimally allocating tasks/parts to workstations within the domain of cycle time and precedence relationship constraints. Characteristics of a U-shaped disassembly line give this layout more chances to find optimal tasks assignment. A mixed-integer non-linear programming model (MINLP) with four different objectives and constraints can be formulated to solve such problem. However, since the DLBP is an NP-hard problem, a novel meta-heuristic algorithm called invasive weed optimization algorithm (IWO) is applied on a straight-line and a U-shaped disassembly line separately. IWO is based on the concept of natural selection (survival of the fittest). Two sets of instances are applied to test the performance of the proposed IWO algorithm. Case studies show that the proposed MINLP model can find optimal solution(s) for small-size instances, and the U-shaped disassembly line performs better than the traditional straight-line disassembly line. A comparative study demonstrates that the proposed IWO algorithm is superior in comparison to other meta-heuristic algorithms reported in the literature.

**KEYWORDS:** Remanufacturing, Disassembly Line Balancing, U-Shaped Disassembly line, Invasive Weed optimization (IWO).

Date of Submission: 12-06-2022

| Date of acceptance: | 26-06-2022 |
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## I. INTRODUCTION

Manufacturing prosperity greatly helps the development of society and technology at some degree. One obvious situation is an increasing number of products are manufactured much faster than ever before [1]. Especially using electronic and electricity products are becoming an important part of daily life of individuals. One unavoidable problem which is troubling global individuals and counties is the number of waste products are getting extremely large. The concept of environmentally conscious manufacturing and product recovery was first highlighted by Gungor and Gupta [2]. which aspires to add green manufacturing to the whole life cycle of a product. With the sustainable development and green manufacturing conscious are becoming a responsibility of industry and society [3], landfilling as a traditional way dealing with waste problem is not widely usable. Product recovery is a smart strategy which adding green concept into waste problem [4]. The nature of product recovery is to minimize the amount of waste through different processes which contain reuse, remanufacturing and recycle. Remanufacturing plays an essential role in retrieving valuable parts/materials from end-of-life (EOL) products and create profits step by step. Disassembly is one of the most important steps in remanufacturing, it aims to disassemble EOL products into subassemblies and/or parts. After EOL products entering disassembly process, disassembly tasks are started. Disassembly tasks are operated on a paced disassembly line via linked workstations and operators and/or intelligent robotics are accessed working in the workstation [5]. Therefore, balancing the disassembly line should be getting much more attention.

Disassembly line balancing problem (DLBP) was, for the first time, proposed by research Gungor and Gupta [6], which aims at optimally allocating tasks to workstations with the domain of cycle time constraint and precedence relationship constraint. There are four popular types of a disassembly lines, namely, straight-line, parallel, U-shaped, and two-sided. A U-shaped disassembly line is much more productive and efficient compared to a straight-line configuration since operators and/or intelligent robotics can work across the workstation [7]. Cycle time constraint ensures that there will not happen line stoppage situation and precedence relationship constraint indicate that the sequence rules between disassembly tasks. Sequence dependent relationship is a special type of precedence relationship since it is much more complicated and sequence dependencies should be considered between target tasks [8, 9].

After the pioneering work by Gungor and Gupta [6], DLBP has becoming an active research area and many approaches and heuristics are applied on a disassembly line. Based on the collection data of research Ozceylan et al. [10], DLBP is considered as a multi-criteria decision-making problem [11] by some research. Models and solution approaches contain linear programming [12, 13], non-linear programming [14], heuristic [15, 16], genetic algorithm [17], Greedy algorithm [18], ant colony optimization [19-21], hill climbing, simulated annealing [22], particle swarm optimization [23], artificial bee colony [8], artificial fish swarm optimization [24], small world optimization [25], invasive weed optimization [26], tabu search [27], reinforcement learning technique [28], teaching-learning-based optimization [7], fish school search optimization [29], network-based shortest route model [30], multi-criteria decision-making [31].

The rest of paper is structured as follows: literature review is included in the next section. The section that follows introduces the detailed disassembly line balancing problem and introduces a mixed-integer non-linear programming (MINLP) model and related constrains. This is followed by a section that covers detailed results and comparison of the performance of several algorithms. The last section provides the conclusion and directions for future research.

### II. LITERATURE REVIEW

There are four typical line types of a disassembly line, viz., straight-line, parallel, U-shaped and twosided. Previous studies focus more on a straight-line layout, whereas U-shaped DLBP is not considered that many [10]. In 2008, the first research of U-shaped DLBP was studied by Agrawal and Tiwari [19] and since then, U-shaped layout is getting much more attentions. Exact methods, heuristics, and meta-heuristics are continuing applied on a U-shaped disassembly line. Yao and Gupta [5, 7, 21, 25, 26, 29] has for the first time, introduced five meta-heuristic algorithms on U-shaped layout, viz., cat swarm optimization (CSO), small world optimization (SWO), ant colony optimization (ACO), invasive weed optimization (IWO), teaching-learningbased optimization (TLBO) and fish school search algorithm (FSS) which expand the field of approaches on DLBP. Sequence-dependent U-shaped DLBP (SUDLBP) was first studied in Li, Kucukkoc, and Zhang [9] and iterated local search strategy was used to help. Wang, Gao, and Li [32] and Li and Janardhanan [33] considered partial disassembly on a U-shaped disassembly line. These two studies enlarge the horizon of UDLBP research. One obvious difference between U-shaped and straight line is operators and/or intelligent robotics can work across the workstation, this may improve line efficiency and productivity.

Considering of uncertainty of real-world instances, sequence dependent situation should be taken into account. According to the research Kalayci and Gupta [8], interactions between tasks will affect task processing times which is called sequence-dependent situation. Notice that sequence dependencies between related tasks are known before disassembling.

McGovern and Gupta [14, 15] mathematically proved that DLBP belongs to NP-hard class problem. Therefore, to obtain near-optimal solutions for large-size instances, heuristics and meta-heuristics are continually introduced in DLBP research field. IWO algorithm is a novel optimization meta-heuristic algorithm which was originally inspired from the nature of weed. Great searching ability makes IWO algorithm is suitable in solving DLBP. For all reasons above, the main contributions to the literature are listed as follows:

(1) Considering of the evaluation of one objective is nonlinear, a mixed-integer nonlinear programming (MINLP) mathematical model is formulated to help solve multi-objective U-shaped DLBP.

(2) Invasive weed optimization algorithm (IWO), has for the first time, applied to help find nearoptimal solutions of sequence-dependent U-shaped DLBP (SUDLBP). It has a great ability to get a suitable balance between exploration and exploitation.

(3) A comprehensive comparative study is conducted on two sets of instances in this paper to evaluate the performance of developed MINLP model and the proposed IWO algorithm. The first instance set contains two small-size cases, and the second instance set includes 47 cases and many of them are large-size instances. Computational tests show that U-shaped disassembly line has greater performance for line smoothness and number of workstations compared with traditional straight-line disassembly line. Total of 10 algorithms are involved to compare the performance of IWO algorithm, and the comparative study demonstrates that the proposed IWO algorithm outperforms other meta-heuristic algorithms on many aspects.

## III. PROBLEM DEFINITION

This section first introduces sequence-dependent U-shaped DLBP (SUDLBP) and then presents the proposed MINLP model and detailed constraints.

#### 3.1 Problem description

DLBP is much more complicated than assembly line balancing problem (ALBP). One reason for that is the precedence relationship in ALBP is only AND precedence relationship, but in DLBP, especially real-world instances, there may exist AND precedence, OR precedence, and complex AND/OR precedence relationships. One task can be disassembled only when all its AND predecessors has been disassembled or at least one of its OR predecessors has been moved based on its precedence relationship. Fig. 1 presents a small-size instance, task 2 and task 3 are OR predecessors of task 4 and task 3 and task 4 are AND predecessors of task 5. To optimally allocate disassembly tasks on workstations, a suitable and efficient model should be proposed.



Fig. 1. Precedence relationship of a 5-part instance

#### **3.2 Mathematical model**

This section presents a mixed-integer non-linear programming model with core constraints. Before introducing the MINLP model, assumptions and notations should be presented. The assumptions are as follows:

- 1. EOL products are only one type and number of products is enough.
- 2. Products should be disassembled completely.
- 3. Task processing time is known and deterministic.
- 4. Task failure is not considered.

The notations and decision variables utilized in the model are given as follows.

| Notations             |  |
|-----------------------|--|
| i,j                   | Task index, $i, j = 1, 2,, N$  |
| М                     | Number of workstations   |
| m                     | Workstation (sub-station) index, $m = 1, 2,, 2M$   |
| $t_i$                 | Processing/removal time of task i  |
| h <sub>i</sub>        | Binary variable, 1, if task i is hazardous; 0, otherwise                                   |
| $d_i$                 | Demand value of task j   |
| ANDP(i)               | Set of AND predecessor of task i   |
| ORP(i)                | Set of OR predecessor of task i  |
| СТ                    | Cycle time   |
| $T_m$                 | Total task processing times of workstation m   |
| $sd_{ij}$             | Sequence dependent time between task j and task i  |
| F <sub>a</sub>        | Objective function, $a = 1,2,3,4$  |
| Decision variables    |  |
| $x_{im}$              | Binary variable, 1, if task i is assigned to sub-station m; 0, otherwise                   |
| $x'_{imi}$            | Binary variable, 1, if task is assigned to sub-station m and is operated before task j; 0, |
|                       | otherwise  |
| W <sub>ij</sub>       | Binary variable, 1, if task i is operated before task j; 0, otherwise                      |
| ws <sub>m</sub>       | Binary variable, 1, if workstation m is opened; 0, otherwise                               |
| <i>s</i> <sub>i</sub> | Position number of task <i>i</i> in sequence   |

Notice that the reason why the maximum amount of m is 2\*M is that on a U-shaped line, one workstation has two directions which are entrance side and exit side, therefore, for computation, one workstation is divided into two sub-stations. A feasible solution of a supposed 8-part instance is shown in Fig.2. In Fig.2, four workstations are divided into 8 sub-stations, therefore M = 4, N = 8, e.g., workstation 1 has two sub-stations which are sub-station 1 and sub-station 8. The sequence of this feasible solution is 1, 3, 6, 4, 8, 7, 2, 5.



Fig.2 A feasible solution on a U-shaped disassembly line

There are four different objective functions in this paper, viz., minimizing number of workstations, increasing line smoothness, removing hazardous part early, and removing high demand part early. Objective functions are presented as follows:

## **Objectives:**

$$\begin{array}{ll} \min F_{1} &= \sum_{m=1}^{M} ws_{m} & (1) \\ \min F_{2} &= \sum_{m=1}^{M} (CT - T_{m})^{2} & (2) \\ \min F_{3} &= \sum_{i=1}^{N} (s_{i} * h_{i}) & (3) \\ \min F_{4} &= \sum_{i=1}^{N} (s_{i} * d_{i}) & (4) \end{array}$$

The first objective is to minimize the number of workstations which is a cost-based consideration. Equation (2) is a non-linear function with the goal of optimally increasing line smoothness. Equation (3) presents removal of hazardous part(s) early and equation (4) tries to remove high demand part(s) early. There are two popular ways to classify optimal or near-optimal solutions, viz., pareto optimal strategy [5, 7, 21, 25, 26, 29] and hierarchy method. In this paper, hierarchy method is utilized to compare near-optimal solutions and  $F_1$ has the highest priority and  $F_2$  weighs lower than  $F_1$ .

**Constraints:** 

$$\begin{split} \sum_{m=1}^{M} (x_{im} + x_{i,2M+1-m}) &= 1 \tag{5} \\ \sum_{i=1}^{N} (x_{im} + x_{i,2M+1-m}) &\geq 1 \tag{6} \\ CT &\geq T_m \tag{7} \\ x_{im} &\leq \sum_{n=1}^{m} x_{jn} \quad \forall i,m; \; \forall j \in ANDP(i) \tag{8} \\ x_{im} &\leq \sum_{i \in OPP(i)} \sum_{m=1}^{m} x_{in} \quad \forall m, \forall i \in ORPT \tag{9} \end{split}$$

$$\begin{split} & w_{ij} + w_{ji} = 1 \quad \forall i, j \text{ and } i < j (10) \\ & T_m = \sum_{i=1}^N t_i \times \left( x_{im} + x_{i,2M+1-m} \right) + \sum_{i=1}^N \sum_{j=1}^N s d_{ji} \times \left( x'_{imj} + x'_{i,2M+1-m,j} \right) \quad \forall i, j (11) \\ & s_i = N - \sum_{j=1}^N w_{ij} \forall i (12) \end{split}$$

Constraint (5) and (6) consider the situation of a workstation, they ensure that one task can only be operated in one sub-station and one sub-station can disassemble one or more tasks, separately. Constraint (7) strictly ensures that line stoppage will not happen which is the cycle time constraint. Constraint (8) and (9) consider different types of precedence relationship and these constraints ensure that this MINLP model can solve complicated precedence relationship problem. Constraint (10) determines the value of  $w_{ij}$ , if  $w_{ij} = 1$ , task i will be disassembled before task j. Constraint (11) and (12) are the calculation of total task processing times of a sub-station and sequence number respectively.

## IV. INVASIVE WEED OPTIMIZATION ALGORITHM (IWO)

Since DLBP belongs to NP-hard class, therefore dealing with large-size instances, meta-heuristic algorithms perform strong searching ability and can find near-optimal solutions in a relative short computational time. This section presents encoding and decoding procedures of IWO algorithm. IWO was originally proposed in research [34] which has a strong global and local searching ability. The basic searching procedure of IWO are as follows:

Step 1: Initialize randomly generated weeds in the entire search space.

Step 2: Evaluate fitness of the whole population members.

Step 3: Allow each population member to produce a few seeds with better population members produce more seeds (i.e., reproduction).

Step 4: The generated seeds are distributed over the search space by normally distributed random numbers with mean equal to zero but varying variance (i.e., spatial dispersal).

Step 5: When the weed population exceeds the upper limit, perform competitive exclusion. Step 6: Check the termination criteria.

## 4.1 Encoding and decoding

In this paper, the encoding of task permutation is same with research Kalayci and Gupta [8, 20, 22, 23, 27]; Li, Kucukkoc, and Zhang [9]. Table 1 and Fig. 3 present information and precedence relationship of an 8-part PC instance respectively, which is acquired from research Kalayci and Gupta [27]. Dashed line in Fig. 3 represents sequence-dependent relationship should be considered between connected tasks. Sequence dependencies of this instance are provided as follows:  $sd_{23} = 2$ ,  $sd_{32} = 4$ ,  $sd_{56} = 1$ ,  $sd_{65} = 3$ . Task assignment of one feasible solution of this small-size instance is shown in Fig. 4.

|      |              | <b>_</b>          |                 |        |
|------|--------------|-------------------|-----------------|--------|
| Task | Part title   | Task removal time | Hazardous index | Demand |
| 1    | PC top cover | 14                | No              | 360    |
| 2    | Floppy drive | 10                | No              | 500    |
| 3    | Hard drive   | 12                | No              | 620    |
| 4    | Back plane   | 18                | No              | 480    |
| 5    | PCI cards    | 23                | No              | 540    |
| 6    | RAM modules  | 16                | No              | 750    |
| 7    | Power supply | 20                | No              | 295    |
| 8    | Motherboard  | 36                | No              | 720    |

Table 1. Information of the 8-part PC instance



Fig. 3. Precedence relationship of the 8-part PC instance





As shown in Fig. 4, the task permutation is 1, 2, 3, 6, 5, 4, 7, 8, but the task sequence is 1, 2, 3, 6, 5, 8, 7, 4, which are different. Therefore, a decoding procedure of IWO is proposed to help transfer task permutation into task sequence. For this small-size instance, Table 2 and Table 3 presents objective values and calculation processes of 4 objectives. Task 1, 2, and 3 are assigned at sub-station 1, task 6 and 5 are allocated at sub-station 2, task 8 is disassembled at sub-station 4, and task 7 and 4 are operated at sub-station 6. The number of workstations is 4, and based on the idle times of each workstation, the value of minimizing total of idle times is

20. Since there is no hazardous task, value of the third objective is 0. According to the model, the value of removing high demand part early is 19145.

| Workstation number | Sub-station number | Task number | Task processing time | Total task processing | Idle time |
|--------------------|--------------------|-------------|----------------------|-----------------------|-----------|
|                    |                    |             |                      | time                  |           |
| Workstation 1      | Sub-station 1      | 1,2,3       | 14,10+4,12           | 40                    | 0         |
|                    | Sub-station 8      | -           | -                    |                       |           |
| Workstation 2      | Sub-station 2      | 6,5         | 16+1,23              | 40                    | 0         |
|                    | Sub-station 7      | -           | -                    |                       |           |
| Workstation 3      | Sub-station 3      | -           | -                    | 38                    | 2         |
|                    | Sub-station 6      | 7,4         | 20,18                |                       |           |
| Workstation 4      | Sub-station 4      | 8           | 36                   | 36                    | 4         |
|                    | Sub-station 5      | -           | -                    |                       |           |

Table 2. Task allocation of a feasible solution for 8-part PC instance

| Table 3. Objective values and calculation p | processes of the feasible solution |
|---|------------------------------------|
|---|------------------------------------|

| Objective number | Objective value   |
|------------------|---|
| $F_1$            | 4   |
| $F_2$            | $0 + 0 + 2^2 + 4^2 = 20$  |
| F <sub>3</sub>   | 0 (No hazardous task)   |
| $F_4$            | $1 \times 360 + 2 \times 500 + 3 \times 620 + 4 \times 750 + 5 \times 540 + 6 \times 720$ |
|                  | $+7 \times 295 + 8 \times 480 = 19145$  |

The decoding procedure in SUDLBP is different from that in SDLBP, since workstations are divided into sub-stations. Detailed decoding procedure of SUDLBP is presented in Algorithm 1 as follows.

#### Algorithm 1. Decoding process for SUDLBP

Start

Step 1: If all tasks are assigned, terminate procedure; otherwise, execute step 2.

- Step 2: Open a new workstation.
- Step 3: Add task(s), whose predecessor(s) has been assigned to the entrance side, to the available task set  $A_{en}$ ; Add task(s), whose successor(s) has been assigned to the exit side, to the available task set  $A_{ex}$ .
- Step 4: Add the task in  $A_{en}$  to the assignable task set  $AS_{en}$  on the entrance side with the domain of cycle time constraint; Add the task in  $A_{ex}$  to the assignable task set  $AS_{ex}$  on the exit side with the domain of cycle time constraint. % For an assignable task, it can be assigned only the total task processing time of this workstation is less than or equal to the given cycle time with the considering of sequence dependency.

Step 5: If both two assignable task sets  $AS_{en}$  and  $AS_{ex}$  are empty, go back to step 1; otherwise, execute step 6.

Step 6: Select the task with higher priority of task permutation and allocate it to the entrance or exit side based on the situation; go back to step 3.

End

## V. COMPUTATIONAL STUDY AND RESULTS

Two instance sets are utilized in this section to help test the performance of IWO algorithm and the proposed model. The first instance set contains two small-size instances which are taken from previous research Kalayci and Gupta [8]. 47 instances are concluded in the second instance set. The smallest-size instance (Mertens) has 7 tasks, and the largest-size instance (Barthol 2) has 148 tasks. Also, the comparation results of traditional straight-line and U-shaped line are presented. Moreover, IWO algorithm is compared with 9 other algorithms which include hill-climbing algorithm (HC) [14, 15], late acceptance hill-climbing algorithm (LAHC) [35], simulated annealing algorithm (SA), tabu search algorithm (TS), genetic algorithm (GA), artificial bee colony algorithm (ABC), bee algorithm (BA), particle swarm optimization (PSO), and iterated local search optimization (ILS).

#### 5.1 Case study

There are two instances in this section which are 10-part instance (P10) and 25-part telephone instance (P25). Information of two instances is acquired from research Kalayci and Gupta [8]. Table 4 and Fig. 5 present related information of P10 instance. Also, sequence dependencies of P10 instance are as follows:  $sd_{1,4} = 1$ ,  $sd_{4,1} = 4$ ,  $sd_{2,3} = 2$ ,  $sd_{3,2} = 3$ ,  $sd_{4,5} = 4$ ,  $sd_{5,4} = 2$ ,  $sd_{5,6} = 2$ ,  $sd_{6,5} = 4$ ,  $sd_{6,9} = 3$ , and  $sd_{9,6} = 1$ . The proposed IWO algorithm is applied on straight-line and U-shaped line separately and tested on each line type 20 times. The cycle time for P10 is predetermined as 40. Table 5 clearly presents that the best value of  $F_1$  is 5 in both line types, whereas U-shape line obtains smaller value on  $F_2$ . Since hierarchy method is applied in this

paper, it is obvious that U-shaped layout performs better. As the standard deviation of all objectives are 0.00, it might be concluded that IWO is robust in solving this instance.

| Table 4. Data of 10-part instance |                   |                 |        |  |  |  |  |
|-----------------------------------|-------------------|-----------------|--------|--|--|--|--|
| Task number                       | Part removal time | Hazardous index | Demand |  |  |  |  |
| 1                                 | 14                | No              | 0      |  |  |  |  |
| 2                                 | 10                | No              | 500    |  |  |  |  |
| 3                                 | 12                | No              | 0      |  |  |  |  |
| 4                                 | 17                | No              | 0      |  |  |  |  |
| 5                                 | 23                | No              | 0      |  |  |  |  |
| 6                                 | 14                | No              | 750    |  |  |  |  |
| 7                                 | 19                | Yes             | 295    |  |  |  |  |
| 8                                 | 36                | No              | 0      |  |  |  |  |
| 9                                 | 14                | No              | 360    |  |  |  |  |
| 10                                | 10                | No              | 0      |  |  |  |  |



Fig. 5. Precedence relationship of P10

Table 5. Results for P10 instance by IWO algorithm

| Line type | Algorithm | Evaluation | $F_1$ | F <sub>2</sub> | $F_3$ | $F_4$   |
|-----------|-----------|------------|-------|----------------|-------|---------|
| SDLBP     | IWO       | Best value | 5     | 67             | 5     | 9605    |
|           |           | Avg. value | 5.00  | 67.00          | 5.00  | 9605.00 |
|           |           | S. D       | 0.00  | 0.00           | 0.00  | 0.00    |
| SUDLBP    | IWO       | Best value | 5     | 61             | 6     | 8880    |
|           |           | Avg. value | 5.00  | 61.00          | 6.00  | 8880.00 |
|           |           | S. D       | 0.00  | 0.00           | 0.00  | 0.00    |

The second case is containing 25 parts and the cycle time of P25 instance is 18. Sequence dependencies of P25 instance are shown as follows:  $sd_{4,5} = 2$ ,  $sd_{5,4} = 1$ ,  $sd_{6,7} = 1$ ,  $sd_{7,6} = 2$ ,  $sd_{6,9} = 2$ ,  $sd_{9,6} = 1$ ,  $sd_{7,8} = 1$ ,  $sd_{8,7} = 2$ ,  $sd_{13,14} = 1$ ,  $sd_{14,13} = 2$ ,  $sd_{14,15} = 2$ ,  $sd_{15,14} = 1$ ,  $sd_{20,21} = 1$ ,  $sd_{21,20} = 2$ ,  $sd_{22,25} = 1$ , and  $sd_{25,22} = 2$ . Fig. 6 and Table 6 show related information of P25 instance. The proposed IWO algorithm was applied on a U-shaped line and a straight line 20 times separately.



Fig. 6. Precedence relationship of P25 instance

| Task number | Part name       | Part removal time | Hazardous index | Demand value |  |  |  |  |  |
|-------------|-----------------|-------------------|-----------------|--------------|--|--|--|--|--|
| 1           | Antenna         | 3                 | 1               | 4            |  |  |  |  |  |
| 2           | Battery         | 2                 | 1               | 7            |  |  |  |  |  |
| 3           | Antenna guide   | 3                 | 0               | 1            |  |  |  |  |  |
| 4           | Bolt (Type 1) A | 10                | 0               | 1            |  |  |  |  |  |

 Table 6. Database for P25 instance

| 5  | Bolt (Type 1) B   | 10 | 0 | 1 |
|----|-------------------|----|---|---|
| 6  | Bolt (Type 2) 1   | 15 | 0 | 1 |
| 7  | Bolt (Type 2) 2   | 15 | 0 | 1 |
| 8  | Bolt (Type 2) 3   | 15 | 0 | 1 |
| 9  | Bolt (Type 2) 4   | 15 | 0 | 1 |
| 10 | Clip              | 2  | 0 | 2 |
| 11 | Rubber Seal       | 2  | 0 | 1 |
| 12 | Speaker           | 2  | 1 | 4 |
| 13 | White Cable       | 2  | 0 | 1 |
| 14 | Red/Blue Cable    | 2  | 0 | 1 |
| 15 | Orange Cable      | 2  | 0 | 1 |
| 16 | Metal Top         | 2  | 0 | 1 |
| 17 | Front Cover       | 2  | 0 | 2 |
| 18 | Back Cover        | 3  | 0 | 2 |
| 19 | Circuit Board     | 18 | 1 | 8 |
| 20 | Plastic Screen    | 5  | 0 | 1 |
| 21 | Keyboard          | 1  | 0 | 4 |
| 22 | LCD               | 5  | 0 | 6 |
| 23 | Sub-keyboard      | 15 | 1 | 7 |
| 24 | Internal IC Board | 2  | 0 | 1 |
| 25 | Microphone        | 2  | 1 | 4 |

From Table 7, it is clear that solutions on U-shaped line performs better than that on straight-line layout, especially considering removing hazardous and high demand parts early. Again, for the first two objectives, IWO obtains the same best results reported in Li, Kucukkoc, and Zhang [9], this illustrates that IWO is effective in solving SUDLBP. Also, U-shaped layout indeed can improve line efficiency and productivity in some respects.

Table 7. Results of P25 for two layouts

| Line type | Algorithm | Evaluation | $F_1$ | $F_2$ | F <sub>3</sub> | $F_4$  |
|-----------|-----------|------------|-------|-------|----------------|--------|
| SDLBP     | IWO       | Best value | 10    | 9     | 80             | 925    |
|           |           | Avg. value | 10.00 | 9.00  | 80.00          | 925.00 |
|           |           | S. D       | 0.00  | 0.00  | 0.00           | 0.00   |
| SUDLBP    | IWO       | Best value | 10    | 9     | 76             | 910    |
|           |           | Avg. value | 10.00 | 9.00  | 77.84          | 914.80 |
|           |           | S. D       | 0.00  | 0.00  | 1.61           | 5.94   |

#### 5.2 Comparative study

This section first compares IWO algorithm with genetic algorithm with variable neighborhood search method (VNSGA) [17] and iterated local search approach (ILS) [9] on two aspects. Best results of three algorithms and listed in Table 8. Notice that, in Table 8, results for VNSGA and ILS algorithm are taken from above mentioned research and the first two objectives are taken into consideration.

| Table 6. Comparison between VINSGA, ILS and IWO |    |      |               |           |        |          |       |          |        |          |       |          |
|---|----|------|---------------|-----------|--------|----------|-------|----------|--------|----------|-------|----------|
| Instance  | Ν  | СТ   | VNSC<br>(SDL) | GA<br>BP) | ILS (S | SDLBP)   | IWO   | (SDLBP)  | ILS (S | UDLBP)   | IWO ( | SUDLBP)  |
|   |    |      | $F_1$         | $F_2$     | $F_1$  | $F_2$    | $F_1$ | $F_2$    | $F_1$  | $F_2$    | $F_1$ | $F_2$    |
| Mertens   | 7  | 7    | 5             | 10        | 5      | 10       | 5     | 10       | 5      | 10       | 5     | 10       |
| Bowman  | 8  | 20   | 5             | 149       | 5      | 149      | 5     | 149      | 4      | 13       | 4     | 13       |
| Jaeschke  | 9  | 7    | 7             | 26        | 7      | 28       | 7     | 28       | 7      | 28       | 7     | 26       |
| Jackson   | 11 | 10   | 5             | 6         | 5      | 6        | 5     | 6        | 5      | 4        | 5     | 4        |
| Mansoor   | 11 | 94   | 2             | 5         | 2      | 5        | 2     | 5        | 2      | 5        | 2     | 5        |
| Mitchell  | 21 | 15   | 8             | 31        | 8      | 43       | 8     | 31       | 8      | 29       | 8     | 29       |
| Roszieg   | 25 | 16   | 8             | 5         | 8      | 5        | 8     | 5        | 8      | 3        | 8     | 3        |
| Heskiaoff                                       | 28 | 216  | 5             | 628       | 5      | 630      | 5     | 628      | 5      | 628      | 5     | 628      |
| Buxey   | 29 | 30   | 12            | 118       | 12     | 122      | 12    | 122      | 11     | 6        | 11    | 6        |
| Lutzl   | 32 | 2357 | 7             | 8.13E+05  | 7      | 8.47E+05 | 7     | 8.53E+05 | 7      | 7.99E+05 | 7     | 8.07E+05 |
| Gunther   | 35 | 41   | 14            | 1519      | 14     | 1735     | 14    | 1759     | 12     | 13       | 12    | 13       |
| Kilbridge                                       | 45 | 62   | 9             | 6         | 9      | 6        | 9     | 6        | 9      | 6        | 9     | 6        |
| Hahn  | 53 | 2806 | 6             | 1.87E+06  | 6      | 1.91E+06 | 6     | 1.90E+06 | 5      | 6        | 5     | 6        |
| Tonge   | 70 | 168  | 22            | 2152      | 22     | 1756     | 22    | 1962     | 22     | 1672     | 22    | 1720     |
| Tonge   | 70 | 170  | 22            | 3002      | 22     | 2660     | 22    | 2730     | 21     | 204      | 21    | 568      |
| Tonge   | 70 | 173  | 22            | 5196      | 21     | 1081     | 22    | 5196     | 21     | 745      | 21    | 891      |
| Tonge   | 70 | 179  | 21            | 3459      | 20     | 312      | 21    | 2304     | 20     | 262      | 20    | 294      |
| Tonge   | 70 | 182  | 20            | 968       | 20     | 912      | 20    | 956      | 20     | 854      | 20    | 882      |
| Wee-Mag   | 75 | 46   | 35            | 983       | 34     | 399      | 34    | 385      | 34     | 349      | 34    | 343      |
| Wee-Mag   | 75 | 47   | 33            | 148       | 33     | 116      | 33    | 122      | 33     | 106      | 33    | 112      |

Table 8. Comparison between VNSGA, ILS and IWO

| Invasive Weed Op | otimization Algorithm | for Solving Multi-Ob | jective Sequence-Dependent |
|------------------|-----------------------|----------------------|----------------------------|
|------------------|-----------------------|----------------------|----------------------------|

|           | r   |       | r  |          |    |          |    | -        |    | -        |    |          |
|-----------|-----|-------|----|----------|----|----------|----|----------|----|----------|----|----------|
| Wee-Mag   | 75  | 49    | 32 | 189      | 32 | 163      | 32 | 167      | 32 | 155      | 32 | 159      |
| Wee-Mag   | 75  | 50    | 32 | 347      | 32 | 333      | 32 | 333      | 32 | 327      | 32 | 327      |
| Wee-Mag   | 75  | 52    | 31 | 455      | 31 | 443      | 31 | 455      | 31 | 431      | 31 | 441      |
| Arcus1    | 83  | 3985  | 20 | 9.34E+05 | 20 | 9.22E+05 | 20 | 9.08E+05 | 20 | 8.14E+05 | 20 | 8.12E+05 |
| Arcus1    | 83  | 5048  | 16 | 1.76E+06 | 16 | 1.76E+06 | 16 | 1.76E+06 | 16 | 1.67E+06 | 16 | 1.65E+06 |
| Arcus1    | 83  | 5853  | 14 | 2.79E+06 | 14 | 2.79E+06 | 14 | 2.79E+06 | 13 | 1.16E+04 | 13 | 1.15E+05 |
| Arcus1    | 83  | 6842  | 12 | 4.26E+06 | 12 | 4.25E+06 | 12 | 4.19E+06 | 12 | 3.43E+06 | 12 | 3.41E+05 |
| Arcus1    | 83  | 7571  | 11 | 5.37E+06 | 11 | 5.54E+06 | 11 | 5.37E+06 | 11 | 5.37E+06 | 11 | 5.37E+06 |
| Arcus1    | 83  | 8412  | 10 | 7.09E+06 | 10 | 7.83E+06 | 10 | 7.17E+06 | 10 | 7.93E+06 | 10 | 7.09E+06 |
| Arcus1    | 83  | 8898  | 9  | 2.14E+06 | 9  | 2.15E+06 | 9  | 2.14E+06 | 9  | 2.13E+06 | 9  | 2.12E+06 |
| Arcus1    | 83  | 10816 | 8  | 1.49E+07 | 8  | 3.75E+07 | 8  | 1.39E+07 | 7  | 1.10E+01 | 7  | 1.09E+07 |
| Lutz2     | 89  | 15    | 34 | 63       | 34 | 61       | 34 | 63       | 33 | 10       | 33 | 10       |
| Lutz3     | 89  | 150   | 12 | 2050     | 12 | 2256     | 12 | 2230     | 11 | 6        | 11 | 6        |
| Mukherjee | 94  | 201   | 23 | 12057    | 23 | 14853    | 23 | 12975    | 21 | 13       | 21 | 13       |
| Mukherjee | 94  | 301   | 15 | 10137    | 15 | 10137    | 15 | 10137    | 14 | 6        | 15 | 2107     |
| Arcus2    | 111 | 5755  | 27 | 2.58E+06 | 27 | 2.40E+06 | 27 | 2.36E+06 | 27 | 1.06E+06 | 27 | 1.04E+06 |
| Arcus2    | 111 | 7520  | 21 | 3.00E+06 | 21 | 2.97E+06 | 21 | 2.99E+06 | 21 | 2.75E+06 | 21 | 2.81E+06 |
| Arcus2    | 111 | 8847  | 18 | 4.38E+06 | 18 | 4.59E+06 | 18 | 4.41E+06 | 18 | 4.41E+06 | 18 | 4.40E+06 |
| Arcus2    | 111 | 10027 | 16 | 6.33E+06 | 16 | 6.39E+06 | 16 | 6.33E+06 | 16 | 6.42E+06 | 16 | 6.31E+06 |
| Arcus2    | 111 | 10743 | 15 | 7.76E+06 | 15 | 7.82E+06 | 15 | 7.79E+06 | 15 | 7.81E+06 | 15 | 7.76E+06 |
| Arcus2    | 111 | 11378 | 14 | 5.76E+06 | 14 | 5.72E+06 | 14 | 5.72E+06 | 14 | 5.68E+06 | 14 | 5.68E+06 |
| Arcus2    | 111 | 11570 | 14 | 9.86E+06 | 14 | 1.02E+07 | 14 | 9.90E+06 | 14 | 9.63E+06 | 14 | 9.60E+06 |
| Arcus2    | 111 | 17067 | 9  | 1.14E+06 |
| Barthol2  | 148 | 85    | 52 | 906      | 51 | 293      | 51 | 365      | 51 | 243      | 51 | 289      |
| Barthol2  | 148 | 89    | 50 | 1174     | 49 | 425      | 49 | 573      | 48 | 74       | 48 | 97       |
| Barthol2  | 148 | 91    | 49 | 1179     | 48 | 504      | 48 | 464      | 47 | 67       | 47 | 65       |
| Barthol2  | 148 | 95    | 47 | 1279     | 46 | 454      | 46 | 448      | 45 | 53       | 45 | 52       |

From Table 8, IWO algorithm is applied on U-shaped line and straight line separately. It is clear that on a straight-line layout, IWO found 42 same and 5 smaller values compared with VNSGA, and IWO obtained 45 same objective values compared with ILS considering minimizing number of workstations. Also, for increasing line smoothness, IWO found 18 same and 19 better values compared with VNSGA, and IWO obtained 14 same and 19 better results compared with ILS. For SUDLBP, IWO found 46 same and 1worse objective values on  $F_1$ , and 18 same and 16 better results on  $F_2$  compared with ILS. Based on comparation results, it might be concluded that IWO has a superior performance, and it is observed that U-shaped disassembly line performs much better than traditional straight-line layout especially on large-size instances.

| Instance  | Ν  | СТ   | HC    | LAHC  | SA    | TS    | GA    | ABC   | BA    | PSO   | ILS  | IWO  |
|-----------|----|------|-------|-------|-------|-------|-------|-------|-------|-------|------|------|
| Mertens   | 7  | 7    | 5     | 5     | 5     | 5     | 5     | 5     | 5     | 5     | 5    | 5    |
| Bowman    | 8  | 20   | 4     | 4     | 4     | 4     | 4     | 4     | 4     | 4     | 4    | 4    |
| Jaeschke  | 9  | 7    | 7     | 7     | 7     | 7     | 7     | 7     | 7     | 7     | 7    | 7    |
| Jackson   | 11 | 10   | 5     | 5     | 5     | 5     | 5     | 5     | 5     | 5     | 5    | 5    |
| Mansoor   | 11 | 94   | 2     | 2     | 2     | 2     | 2     | 2     | 2     | 2     | 2    | 2    |
| Mitchell  | 21 | 15   | 8     | 8     | 8     | 8     | 8     | 8     | 8     | 8     | 8    | 8    |
| Roszieg   | 25 | 16   | 8     | 8     | 8     | 8     | 8     | 8     | 8     | 8     | 8    | 8    |
| Heskiaoff | 28 | 216  | 5     | 5     | 5     | 5     | 5     | 5     | 5     | 5     | 5    | 5    |
| Buxey     | 29 | 30   | 11    | 11.05 | 11    | 11    | 11    | 11.15 | 11    | 11    | 11   | 11   |
| Lutzl     | 32 | 2357 | 7     | 7     | 7     | 7     | 7     | 7     | 7     | 7     | 7    | 7    |
| Gunther   | 35 | 41   | 12    | 12    | 12    | 12.15 | 12    | 12    | 12    | 12    | 12   | 12   |
| Kilbridge | 45 | 62   | 9     | 9     | 9     | 9     | 9     | 9     | 9     | 9     | 9    | 9    |
| Hahn      | 53 | 2806 | 5.7   | 5.65  | 5.85  | 5.5   | 6.0   | 5.85  | 5.65  | 5.85  | 5.2  | 5.2  |
| Tonge     | 70 | 168  | 22    | 22    | 22    | 22    | 22.05 | 22    | 22.05 | 22    | 22   | 22   |
| Tonge     | 70 | 170  | 21.95 | 21.95 | 22.05 | 21.85 | 21.95 | 22    | 22    | 21.95 | 21.8 | 21.8 |
| Tonge     | 70 | 173  | 21    | 21    | 21.15 | 21    | 21    | 21    | 21    | 21    | 21   | 21   |
| Tonge     | 70 | 179  | 20    | 20    | 20    | 20    | 20    | 20.5  | 20    | 20    | 20   | 20   |
| Tonge     | 70 | 182  | 20    | 20    | 20    | 20    | 20    | 20    | 20    | 20    | 20   | 20   |
| Wee-Mag   | 75 | 46   | 34    | 34    | 34.15 | 34    | 34    | 34.5  | 34.95 | 34.05 | 34   | 34   |
| Wee-Mag   | 75 | 47   | 33    | 33    | 33    | 33    | 33    | 33    | 33    | 33    | 33   | 33   |
| Wee-Mag   | 75 | 49   | 32    | 32    | 32    | 32    | 32    | 32    | 32    | 32    | 32   | 32   |
| Wee-Mag   | 75 | 50   | 32    | 32    | 32    | 32    | 32    | 32    | 32    | 32    | 32   | 32   |
| Wee-Mag   | 75 | 52   | 31    | 31    | 31    | 31.05 | 31    | 31    | 31    | 31    | 31   | 31   |
| Arcus1    | 83 | 3985 | 20    | 20    | 20.4  | 20    | 20    | 20.4  | 20    | 20    | 20   | 20   |
| Arcus1    | 83 | 5048 | 16    | 16    | 16    | 16    | 16    | 16    | 16    | 16    | 16   | 16   |
| Arcus1    | 83 | 5853 | 13    | 13    | 13.4  | 13    | 13.85 | 14    | 13    | 13.7  | 13   | 13   |
| Arcus1    | 83 | 6842 | 12    | 12    | 12    | 12    | 12    | 12    | 12    | 12    | 12   | 12   |
| Arcus1    | 83 | 7571 | 11    | 11    | 11    | 11    | 11    | 11    | 11    | 11    | 11   | 11   |
| Arcus1    | 83 | 8412 | 10    | 10    | 10    | 10    | 10    | 10    | 10    | 10    | 10   | 10   |

 Table 9. Performance of 10 algorithms on the first objective

|--|

| Arcus1    | 83  | 8898  | 9     | 9     | 9     | 9.15 | 9     | 9     | 9     | 9     | 9     | 9    |
|-----------|-----|-------|-------|-------|-------|------|-------|-------|-------|-------|-------|------|
| Arcus1    | 83  | 10816 | 8     | 8     | 8.3   | 8    | 8     | 8     | 8     | 8     | 7.8   | 8    |
| Lutz2     | 89  | 15    | 33    | 33    | 33.3  | 33   | 33.5  | 33    | 33.3  | 33    | 33    | 33   |
| Lutz3     | 89  | 150   | 11    | 11    | 11    | 11   | 11.4  | 11.25 | 11    | 11    | 11    | 11   |
| Mukherjee | 94  | 201   | 21.25 | 21.2  | 21.3  | 22   | 21.7  | 22    | 21.75 | 21.75 | 21.25 | 21.2 |
| Mukherjee | 94  | 301   | 14    | 14    | 14.15 | 14.3 | 14.9  | 15.15 | 14.75 | 14.5  | 14    | 15   |
| Arcus2    | 111 | 5755  | 27    | 27    | 27    | 27   | 27    | 27    | 27    | 27    | 27    | 27   |
| Arcus2    | 111 | 7520  | 21    | 21    | 21    | 21   | 21    | 21    | 21    | 21    | 21    | 21   |
| Arcus2    | 111 | 8847  | 18    | 18    | 18    | 18   | 18.15 | 18    | 18    | 18    | 18    | 18   |
| Arcus2    | 111 | 10027 | 16    | 16    | 16    | 16   | 16    | 16    | 16    | 16    | 16    | 16   |
| Arcus2    | 111 | 10743 | 15    | 15    | 15    | 15   | 15    | 15    | 15    | 15    | 15    | 15   |
| Arcus2    | 111 | 11378 | 14    | 14    | 14    | 14   | 14    | 14    | 14    | 14    | 14    | 14   |
| Arcus2    | 111 | 11570 | 14    | 14    | 14    | 14   | 14    | 14    | 14    | 14    | 14    | 14   |
| Arcus2    | 111 | 17067 | 9     | 9     | 9     | 9    | 9     | 9     | 9     | 9     | 9     | 9    |
| Barthol2  | 148 | 85    | 51    | 51    | 51.95 | 51.5 | 51.7  | 51.7  | 51.15 | 51.05 | 51    | 51   |
| Barthol2  | 148 | 89    | 49    | 48.9  | 48.7  | 49   | 49.15 | 49    | 49    | 49.05 | 48.75 | 48.7 |
| Barthol2  | 148 | 91    | 48    | 47.8  | 47.75 | 48   | 48    | 48    | 48    | 48.3  | 47.6  | 47.5 |
| Barthol2  | 148 | 95    | 45.9  | 45.85 | 46.15 | 46   | 45.95 | 46    | 45.7  | 46    | 45.65 | 45.5 |

| Table 10 | . Performance of 1 | 0 algorithms | on the second | objective |
|----------|--------------------|--------------|---------------|-----------|
|          |                    |              |               |           |

| Instance  | Ν   | CT    | HC     | LAHC   | SA     | TS     | GA     | ABC    | BA     | PSO    | ILS    | IWO    |
|-----------|-----|-------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| Mertens   | 7   | 7     | 10     | 10     | 10     | 10     | 10     | 10     | 10     | 10     | 10     | 10     |
| Bowman    | 8   | 20    | 13     | 13     | 13     | 13     | 13     | 13     | 13     | 13     | 13     | 13     |
| Jaeschke  | 9   | 7     | 28     | 28     | 28     | 28     | 28     | 28     | 28     | 28     | 28     | 28     |
| Jackson   | 11  | 10    | 4      | 4      | 4      | 4      | 4      | 4      | 4      | 4      | 4      | 4      |
| Mansoor   | 11  | 94    | 5      | 5      | 5      | 5      | 5      | 5      | 5      | 5      | 5      | 5      |
| Mitchell  | 21  | 15    | 30.7   | 31     | 29.6   | 29.7   | 29.7   | 30.3   | 30.2   | 29.7   | 29.1   | 29.3   |
| Roszieg   | 25  | 16    | 3.2    | 3.9    | 3      | 3.2    | 3      | 3      | 3.5    | 3      | 3      | 3      |
| Heskiaoff | 28  | 216   | 634.8  | 636.4  | 629.7  | 633.4  | 629.7  | 630.3  | 628.7  | 629.5  | 629.1  | 629.0  |
| Buxey     | 29  | 30    | 8.4    | 15.8   | 9.4    | 7.9    | 7.7    | 6.9    | 7.1    | 6.2    | 6.5    | 6.2    |
| Lutzl     | 32  | 2357  | 838157 | 830279 | 836797 | 871356 | 810743 | 814624 | 855693 | 837661 | 804475 | 811792 |
| Gunther   | 35  | 41    | 13     | 13.4   | 14.1   | 13.7   | 14.0   | 13.3   | 13.5   | 13.1   | 13.1   | 13.0   |
| Kilbridge | 45  | 62    | 6.2    | 8.9    | 6.3    | 6.1    | 6      | 6      | 6      | 6.2    | 6      | 6      |
| Hahn      | 53  | 2806  | 1E+06  | 1E+06  | 1E+06  | 997632 | 1E+06  | 932610 | 1E+06  | 964275 | 344411 | 285907 |
| Tonge     | 70  | 168   | 1805.5 | 1811.3 | 2105.6 | 1895.3 | 1796.8 | 1919.3 | 1791.7 | 1765.9 | 1783.0 | 1796.4 |
| Tonge     | 70  | 170   | 2690.9 | 2651.8 | 3037.9 | 2590.6 | 2437.1 | 2985.6 | 3250.5 | 2574.8 | 2159.8 | 2437.9 |
| Tonge     | 70  | 173   | 1088.8 | 1719.7 | 1356.4 | 1089.1 | 992.4  | 1405.3 | 1239.5 | 892.5  | 954.1  | 933.9  |
| Tonge     | 70  | 179   | 325.6  | 518.5  | 442.6  | 397.5  | 1053.4 | 291.4  | 315.8  | 287.4  | 290.8  | 330.5  |
| Tonge     | 70  | 182   | 934    | 1685.7 | 1105.2 | 939.4  | 890.1  | 1207.9 | 971.5  | 934.7  | 879.9  | 904.9  |
| Wee-Mag   | 75  | 46    | 475.4  | 457.5  | 417.4  | 387.2  | 568.3  | 621.3  | 379.1  | 390.6  | 426.7  | 373.4  |
| Wee-Mag   | 75  | 47    | 128.5  | 118.0  | 117.9  | 125.4  | 126.5  | 133.8  | 128.1  | 119.5  | 117.3  | 120.1  |
| Wee-Mag   | 75  | 49    | 159.9  | 159.5  | 159.4  | 162.7  | 160.3  | 174.5  | 156.3  | 167.9  | 159.3  | 160.5  |
| Wee-Mag   | 75  | 50    | 337.8  | 331.5  | 337.2  | 332.9  | 340.5  | 336.6  | 339.1  | 335.7  | 330.5  | 330.9  |
| Wee-Mag   | 75  | 52    | 446.9  | 444.4  | 445.6  | 452.1  | 439.4  | 447.3  | 452.2  | 443.7  | 437.8  | 448.0  |
| Arcus1    | 83  | 3985  | 838896 | 835347 | 893527 | 902607 | 843561 | 839215 | 863780 | 829735 | 827898 | 818734 |
| Arcus1    | 83  | 5048  | 2E+06  |
| Arcus1    | 83  | 5853  | 13515  | 19389  | 2E+06  | 36721  | 19405  | 68927  | 1E+06  | 2E+06  | 12786  | 11974  |
| Arcus1    | 83  | 6842  | 4E+06  | 4E+06  | 3E+06  | 4E+06  |
| Arcus1    | 83  | 7571  | 6E+06  | 6E+06  | 8E+06  | 6E+06  | 6E+06  | 7E+06  | 7E+06  | 6E+06  | 6E+06  | 6E+06  |
| Arcus1    | 83  | 8412  | 1E+07  | 1E+07  | 1E+07  | 1E+07  | 9E+06  | 9E+06  | 9E+06  | 1E+07  | 1E+07  | 9E+06  |
| Arcus1    | 83  | 8898  | 2E+06  |
| Arcus1    | 83  | 10816 | 4E+07  | 4E+07  | 5E+07  | 4E+07  | 4E+07  | 5E+07  | 4E+07  | 4E+07  | 3E+07  | 3E+07  |
| Lutz2     | 89  | 15.0  | 10.3   | 16.5   | 110.9  | 15.2   | 13.7   | 12.0   | 11.3   | 10.7   | 10.1   | 10.5   |
| Lutz3     | 89  | 150   | 6.4    | 10.7   | 302.0  | 6.9    | 7.4    | 87.5   | 6.9    | 473.9  | 6.6    | 6.5    |
| Mukherjee | 94  | 201   | 588.25 | 475.1  | 1749.4 | 1839.7 | 2457.2 | 985.4  | 1624.3 | 2057.9 | 564.35 | 589.4  |
| Mukherjee | 94  | 301   | 14.4   | 16.5   | 3873.1 | 24.8   | 2196.6 | 4237.7 | 6108.3 | 5426.0 | 9.6    | 2457.5 |
| Arcus2    | 111 | 5755  | 1E+06  | 2E+06  | 1E+06  | 1E+06  | 2E+06  | 1E+06  | 1E+06  | 1E+06  | 1E+06  | 1E+06  |
| Arcus2    | 111 | 7520  | 3E+06  |
| Arcus2    | 111 | 8847  | 5E+06  | 5E+06  | 5E+06  | 6E+06  | 5E+06  | 5E+06  | 5E+06  | 5E+06  | 5E+06  | 5E+06  |
| Arcus2    | 111 | 10027 | 7E+06  | 7E+06  | 7E+06  | 7E+06  | 7E+06  | 8E+06  | 7E+06  | 7E+06  | 7E+06  | 7E+06  |
| Arcus2    | 111 | 10743 | 8E+06  | 8E+06  | 9E+06  | 8E+06  | 8E+06  | 9E+06  | 9E+06  | 8E+06  | 8E+06  | 8E+06  |
| Arcus2    | 111 | 11378 | 6E+06  |
| Arcus2    | 111 | 11570 | 1E+07  |
| Arcus2    | 111 | 17067 | 1E+06  |
| Barthol2  | 148 | 85    | 259.8  | 258.4  | 373.5  | 428.4  | 550.1  | 283.9  | 315.4  | 315.0  | 257.4  | 305.2  |
| Barthol2  | 148 | 89    | 371.2  | 346.0  | 371.5  | 420.9  | 573.4  | 309.0  | 853.2  | 462.9  | 294.65 | 287.2  |
| Barthol2  | 148 | 91    | 414.0  | 362.4  | 523.4  | 425.0  | 471.2  | 580.9  | 402.7  | 356.3  | 281.3  | 265.7  |
| Barthol2  | 148 | 95    | 419.4  | 396.95 | 473.2  | 379.4  | 593.1  | 478.5  | 671.3  | 1024.5 | 311.65 | 324.3  |

Table 9 and Table 10 present detailed comparation results of 10 algorithms on a U-shaped disassembly line in terms of  $F_1$  and  $F_2$  respectively. Notice that part data is acquired from related research study and SA, TS, GA, ABC, BA, and PSO are re-implemented 20 times. From Table 9 and Table 10, IWO performs better than many of these algorithms especially on solving large-size instances. In terms of  $F_2$ , IWO obtains 30 best values and part of objective values is same with other results. It is concluded that IWO has a strong searching ability, and it shows superior performance in solving SUDLBP.

#### VII.CONCLUSION

Environmental protection concept is widely accepted in all countries and green manufacturing method gets a great development recently. As an important step in remanufacturing, disassembly is becoming an active research area and DLBP is getting much more attentions. This study provides the first study of applying IWO algorithm on a U-shaped layout with the considering of sequence dependent situation. The encoding and decoding procedures of IWO algorithm help tackle SUDLBP. In the meanwhile, the proposed MINLP model is capable of solving large-size instances.

Based on the case studies and comparative study, U-shaped layout allows more task assignments and has a better performance compared with traditional straight-line layout. In the future, U-shaped, parallel, and two-sided line are worth of studying. Also, it is concluded that IWO algorithm has a strong ability in solve DLBP or even SUDLBP and comparation results illustrate that IWO algorithm is superior especially on increasing line smoothness. Novel meta-heuristic algorithms can be applied on a disassembly and improved previous approaches are of interest for researchers to explore.

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